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IMPROVING THE FUEL ECONOMY OF CLASS 8 MILITARY VEHICLES USING A SMART CRUISE CONTROL ALGORITHM

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ABSTRACT

Connected and automated vehicles (CAVS) have the potential to improve fuel economy by changing the way vehicles are driven. Fuel economy can be improved through a wide range of technologies, many of which do not require Level 5 automation. One of the most promising technologies is a smart cruise control that uses a speed-matching algorithm to account for fuel economy. Accounting for fuel economy in the algorithm leads to different driving behavior than simply matching the driver-entered set speed. This paper describes how such a smart cruise control could be applied to a class 8 vehicle both in simulation and in the actual vehicle on a closed test track. It evaluates the algorithm and describes the correlation procedure used to calibrate the model using test data from the vehicle.

INTRODUCTION

Connected and automated vehicles (CAVS) have the potential to improve fuel economy by changing the way vehicles are driven. Fuel economy can be improved through a wide range of technologies, many of which do not require Level 5 automation. One of the most promising technologies is smart cruise control that uses an algorithm to account for fuel economy, leading to different driving behavior than simply matching the driverentered set speed. The first iteration of such a smart cruise controller in this study was a heuristic control that improved fuel economy by choosing an optimal set speed for the vehicle within a desired tolerance band. It also adjusted the set speed based upon grade information along the route. The general

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heuristic rules were determined based on prior simulation work. This heuristic control strategy was developed and simulated in the software Autonomie, which was developed by Argonne National Laboratory and funded through the U.S. Department of Energy (DOE). Autonomie has a plug-and-play architecture, based on Matlab, Simulink, and Stateflow, that can simulate a single vehicle or a small collection of vehicles on a route.

This smart cruise control was then further refined and calibrated in a hardware-in-theloop (HIL)/software-in-the-loop (SIL) system developed by the Tank Automotive Research and Development Center (TARDEC). Finally, TARDEC implemented the strategy in an instrumented class 8 vehicle and conducted tests on a closed test course where they investigated fuel economy improvements. The test results showed great promise in the technology on certain driving cycles.

In the future, the data collected from the test course will be used to calibrate the vehicle model and develop an optimal controller. During this second phase, a model predictive controller will be developed to look ahead on the route and choose the optimal vehicle speed and gear to maximize fuel economy.

Autonomous vehicles will yield fuel economy improvement over current vehicles, which will assist the U.S. Department of Defense (DOD) in its endeavor to reduce vehicle life cycle costs. To evaluate the potential benefits of using autonomous vehicle technologies to improve fuel economy, a smart cruise controller was developed for a class 8 military vehicle using the principles of model-based design. This controller was evaluated both in the actual vehicle and in simulation.

AUTONOMIE

Autonomie is a vehicle simulation software that predicts performance and acceleration for both light- and heavy-duty vehicles. The vehicle models in Autonomie are written in Matlab, Simulink and Stateflow. The user interface of Autonomie is in C#. Development of Autonomie began in 2007 and was initially performed under a CRADA with General Motors. Figure 1 shows the toplevel view of an Autonomie Simulink model [1].



Figure 1: Top-level Autonomie Model

Figure 2 shows the user interface of Autonomie.

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Figure 2: Autonomie REV15SP1 User Interface

VEHICLES

The purpose of this paper is to demonstrate how fuel economy can be improved if the stock autonomous vehicle control strategy was modified to account for fuel economy. The way a human drives has a considerable effect on fuel economy. Aggressive driving leads to poor fuel economy. Having a control algorithm drive instead of a human affords us the opportunity to optimize driving behavior for fuel economy. This study used two Class 8 vehicles: the M915 A3 and the M915 A5 Line Haul. Both of these vehicles were outfitted with the Autonomous Mobility Applique System (AMAS) developed by Lockheed Martin. The AMAS system provides driver warning/driver assist and leader-follower capabilities; however, the AMAS control was not designed with fuel conservation as a goal. For instance, when in follower mode, the vehicle aggressively applies engine torque and brake to maintain a fixed gap distance. By smoothing the engine torque behavior and allowing more play in gap distance, the vehicle fuel economy could be improved. In addition, if the vehicle acceleration could be slowed when resuming motion after a stop, the fuel economy could be improved. The idea is to focus on different aspects of vehicle control and smooth out the system response so that aggressive driving is replaced with slower, smoother, more fuelefficient driving. Because this control was implemented in the actual vehicles, only two specific modes were selected to improve. Both involved the cruise control functionality of the vehicles.

The first control improvement occurs when initially setting the vehicle speed. When the vehicle cruise speed was set, instead of driving the exact set speed, the smart cruise picked the most efficient vehicle speed within -specified bounds of the set speed. The new speed had to be within specified bounds of the original set speed or the AMAS system would register a fault condition. In addition to adjusting the vehicle speed to obtain a better fuel economy, a route-based, lookahead control was also considered. That is, when the controller detected an approaching change in grade, it would select a new set speed for the vehicle in order to improve the vehicle's overall fuel economy over the route.

The second control improvement occurs when returning to the previous set speed after a stop. This acceleration from stop to set speed was reduced to provide a more gradual acceleration.

We focused on these two modes of operation during this first phase of vehicle controller improvements. The ultimate goal is to improve all modes of autonomous driving, but this will happen during later phases.

SMART CRUISE

A smart cruise control was developed to replace the stock cruise control of the vehicle.

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The main goal for this first phase of the project was to collect data, refine the vehicle model, and use the refined vehicle model to develop a model predictive controller for the full platoon operation, which would be part of the second phase. However, for this initial phase of the project, it was desirable to provide a smart cruise controller that could improve fuel economy, but be a simpler heuristic controller that would be easy to implement in the vehicle and would override the default functionality of the AMAS. The controller is described below.

The basic controller is a PI controller (see Equation 1) with a Kp and Ki set based on the specific vehicle characteristics, such as vehicle mass, of the A3 or A5. Appropriate values were determined in simulation by running an optimization on the model:

$$T_{dmd} = Kp(V_{target} - V) + Ki \int (V_{target} - V)dt$$
(1)

Note that all variables in this equation and all following equations are defined in a table at the end of this paper.

Once the Kp and Ki values were known, we had to determine a method for predicting the

target speed that gives the best fuel economy, that is, the target speed that minimizes the following cost function:

$$V^* = \underset{\mathbf{V}}{\operatorname{arg\,min}} \int_T \dot{m}_{fuel}(V, \theta(t)) dt$$
(2)

We can determine the fuel mass flow rate by starting with the road load at the wheel and projecting it through the powertrain to the engine:

$$T_{dmd} = R_{wheel} (ma + mg(C_{rr0} + C_{rr1}V)\cos(\theta) + \dots$$
$$\frac{1}{2}\delta_{air}AC_dV^2 + mg\sin(\theta))$$
(3)

Next, the torque demand at the engine can be projected through the transmission ratios and efficiencies to the engine:

$$T_{eng} = \frac{T_{dmd}}{\eta_{fd}\eta_{trans}R_{fd}R_{trans}(N_{gear})}_{(4)}$$

The wheel speed can also be projected through the transmission ratios to obtain the engine speed:

$$\omega_{eng} = V \times \frac{R_{fd}R_{trans}(N_{gear})}{R_{wheel}}$$
(5)

The transmission ratio is dependent on the gear number, which was given by a lookup table; this number is essentially a function of normalized torque demand at the wheels and vehicle speed:

$$N_{gear} = Shift(T_{dmd}, V)_{(6)}$$

The fuel rate of the engine can be expressed as a function of engine torque and engine speed:

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$$\dot{m}_{fuel} = f(T_{eng}, w_{eng})_{(7)}$$

Now Equation 3 can be inserted into Equation 4 and 6. Likewise, Equations 4 and 5 can be inserted into Equation 7 to produce an expression for the fuel rate in terms of the vehicle speed, grade and gear number:

$$\dot{m}_{fuel} = f(V, \theta, N_{gear})_{(8)}$$

Substituting Equation 6 into Equation 8 produces the desired expression for fuel mass flow rate appearing in Equation 2. That is, assuming that the vehicle acceleration is negligible. Using this expression and assuming that the vehicle speed must be within a tolerance of the set speed (the speed set by the driver when enabling the cruise control), we can create a lookup table. That is, the additional constraint is as follows:

$$V_{driver} - \Delta V < V^* < V_{driver} + \Delta V$$
⁽⁹⁾

Basically, for a given set speed and grade, an optimum point was found within the tolerance and used as the alternative target speed in the controller map [2-4].

CONTROLLER ADAPTED FOR HIL/SIL TEST BENCH

To use the smart cruise control in the HIL/SIL setup and within the test vehicle, the controller first had to (1) communicate via UDP and (2) run in real time. Both criteria were satisfied using the Simulink Desktop Real-time toolbox from Mathworks. This toolbox provides a real-time kernel that executes a Simulink diagram in real time. The UDP communication was provided through the UDP blockset that comes as part of the Simulink Desktop Real-time toolbox. An example is shown in Figure 4.



Figure 4: Top-Level Smart Cruise Control Diagram Showing UDP Interface

The controller ran in real time at a rate of 100 Hz on a laptop. The controller and the vehicle exchanged three input UDP packets and one output UDP packet. These packets are described in Tables 1, 2, 3, and 4:

Fable 1: Input UD	P Packet	Vehicle Status
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Data in	Description
Packet	
Vehicle	Current speed of the
Speed	vehicle
Target	Desired speed of the
Speed	vehicle (cruise control
	target set speed)
Engine	Current engine speed
Speed	
Engine	Current engine command
Command	
Packet	Packet index to order
Index	packets

Table 2: Input UDP Packet Cruise On

Data in	Description
Packet	

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Engage	Tells controller when cruise
	control is turned on

Table 3: Input UDP Packet Terrain Info

Data in Packet	Description
Terrain Pitch	Current grade

Table	4 :	Output	UDP	Packet	Engine
Comma	and				

Data in Packet	Description
Engine Command	0 to 100 percent
	engine command

CONTROLLER IN VEHICLE

When testing the controller in the vehicle, constraints were added to ensure that the additional controller logic did not throw a fault. One of these constrains required maintaining the packet order, so a packet index had to be added to the input engine command packet, which was then passed through to the outgoing engine command packet. Initially, there were also other constraints on the magnitude of the engine command signal. Because the AMAS control was still active in the vehicle, but being bypassed, the control signal generated by the smart cruise had to fall within certain bounds of the original AMAS signal; otherwise, the system detected a fault condition. Work had to be performed to turn off this constraint to allow more freedom in the commanded engine torque.

TEST DATA COLLECTION

Test data was collected from three sources. First, data was collected from the onboard vehicle J1939 CAN network. This set of signals included engine torque, engine speed, engine command, engine temperature, brake pedal percent, current gear, torque converter lockup state, and engine fuel rate, in addition to many other signals. Second, data was collected from a series of analog sensors. This set of signals included fan speed, radiator in and out temperatures, and a few other signals. In some cases, both an analog sensor and CAN data was available. Finally, fuel rate data was collected from a special fuel rate measurement system spliced into the fuel line of the vehicle. This measurement allowed high-fidelity real-time measurement of the fuel rate. All of this data was collected and uploaded to a secure site using cellular network connectivity.

The A3 and A5 were both tested at the proving grounds Aberdeen on the Automotive Technology Evaluation Facility (ATEF) route and the Churchville C route. The ATEF route is a 4.5-mile circuit on level ground. The test was performed at a set speed of 50 mph in straight portions of the track and at 40 mph in the curved portions of the track. The test was repeated on the gravel loop of the track, which travels alongside the paved track. The Churchville C is a hilly track, 2.4 miles long, with a maximum grade of about 15%. Each track was tested several times. The driver completed a baseline run, along with runs with the AMAS controller and the smart cruise controller. They drove around 230 laps in total, over a period of four days.

TEST DATA ANALYSIS

We compared the baseline test driven by a human to the test using smart cruise. The following figures show smart cruise was able to improve fuel economy on the ATEF cycle.

Because the ATEF route is on level ground, the only method available to improve fuel economy there was to choose a more efficient vehicle speed at which to drive the vehicle. Figure 5 shows that smart cruise consistently chose a slower speed at which to drive the vehicle.

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Figure 6 shows significant fuel savings from driving the vehicle slower. Even though this behavior can be easily replicated by a human driver, this exercise still demonstrates the concept of overriding the default cruise control with different logic to maximize the vehicle's fuel economy.



Figure 7 illustrates the same operation. The smart cruise control chose to operate the vehicle at a lower vehicle speed.



However, in this case the strategy does not result in improved fuel economy; it leads to worse fuel economy. Figure 8 shows the mass of fuel consumed has increased over the lap.



Figure 8: Churchville-C A3 Cumulative Fuel Use: Smart vs. Baseline

Figure 9 shows that the fuel rate is significantly higher for the smart cruise than for the baseline around the 700th meter on the lap.

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Figure 10 shows that the higher fuel rate is related to a greater engine torque demand rather than a less-efficient operating point of the engine. Why is the demand for the smart cruise so high, when the demand for the baseline is much lower?



Baseline, Engine Demand Event 1

Figure 11 shows that the vehicle is beginning to head downhill. This indicates that the controller was not receiving the necessary grade information to make an accurate determination of the required load on the engine. It was later confirmed that this was indeed the case. The controller had issues computing the grade from the elevation data coming off of the CAN because the data was noisier than expected and intermittently unavailable.



Figure 12 shows another mode on the Churchville course for which the fuel rate was higher for the smart cruise controller than for the baseline.



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Figure 13 shows that this occurs because the engine demand again is much higher for the smart cruise.





Figure 14 shows that the event occurs when the vehicle is accelerating from a stop.



Figure 15 shows that the stop occurs on a downhill portion of the lap. Yet again, it seems like the controller, unaware of grade, is overcompensating and demanding too much torque from the engine.



Figure 16 shows the behavior of the smart cruise compared to the baseline for the A5. It exhibited the same driving behavior as for the A3. The smart cruise drove the vehicle at a slower speed.



Figure 17 shows the total fuel consumed.





Cumulative Fuel Use

Figures 18 and 19 compare the smart cruise with the baseline human driver for the A5 on the Churcville C cycle. As for the A3, the smart cruise consumed more fuel because of difficulties with responding to grade.



Figure 18: ATEF A5: Smart vs. Baseline, Vehicle Speed



Another factor which could have lead to worse fuel economy was the lack of control over the gear selection. When in smart cruise mode, the AMAS control still determined the desired gear which could have impared the smart cruise controller. Having control over the gear selection could have allowed the controller to improve the fuel economy of the vehicle.

MODEL CORRELATION

One of the main goals of this first phase of testing was to use the test data from the vehicles to refine the models, so the revised models could be used in the next phase of control development. Therefore, the Autonomie vehicle models for both the A3 and the A5 were updated and correlated with the test data. The modifications to the vehicle models are described next.

Accounting for Wind

The wind speed was recorded during the test and used it in place of the vehicle speed to calculate the air dynamic losses. It was assumed that the recorded wind speed represented the airflow across the vehicle.

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Gear Shifting

There were differences in the gear shifting between the test data and the simulation. These differences were primarily due to engine breaking events that would trigger a downshift in the vehicle. To overcome these differences in gear shifting, the measured gear from the vehicle was injected into the model, so that the rest of the losses in the vehicle model could be compared to the test data.

Accessory Load

The initial average mechanical accessory load was not sufficient for these vehicles and their loading. The fan would turn on frequently to cool the vehicle. To get a better estimate of the mechanical accessory losses, we analyzed each lap to identify conditions when the vehicle was stopped but the engine was still producing power. Using the value of the accessory load while the vehicle was stopped provided a better estimate for the fuel consumption. Figure 20 shows a distribution plot for the A3 mechanical accessory load while the vehicle is stopped during the ATEF cycle. Figure 21 shows the same plot for the A3 on the Churchville-C cycle. Because the Churchville-C cycle is more aggressive, the fan had to turn on more frequently to cool the engine. The air conditioner was also running continuously during the test.



Figure 20: Mechanical Accessory Load Distribution on the ATEF for the A3

CTA-C-A3- Estimated Accessory Load When Vehicle is Stopped



Figure 21: Mechanical Accessory Load Distribution on the Churchville-C for the A3

Rolling Resistance

The ATEF had both a paved and a gravel loop, while the Churchville-C only had a gravel loop. The gravel road surface changed the rolling resistance of the vehicle. To determine the rolling resistance on the gravel road, the model was first correlated on the paved road. The model developed from the paved road was then simulated on the gravel loop. The rolling resistance coefficient was then adjusted until the error between the test fuel consumption and the simulated fuel

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consumption was minimized. This procedure was repeated for each lap, and a histogram of rolling resistance coefficients was created. From this histogram, we obtained a weighted value representing the rolling resistance for the ATEF. We repeated this procedure for the Churchville-C. Figure 22 shows an example histogram computed from the lap data. A least-squares fit was also performed, but the optimization routine yielded a more reasonable value for the coefficient.



Engine Map

A new engine map was created from the test data. The fuel rate data from a selection of laps, from both the ATEF and Churchville-C, were binned as a function of torque and speed. Next, the Mathworks algorithm griddata was used to fit a parametric surface to the data. This surface was smoothed using a Gaussian filter to remove any jagged edges and high-frequency noise. The new engine map yielded a 4 to 5% improvement in the fuel economy prediction.

Correlation Results

After the model was calibrated using the test data, while still preventing over fitting, it

showed good correlation with the test data. Figure 23 shows this for the A3.



Figure 14 shows the correlation between the simulation and the test data for the A5.



n theFigure 25 shows a histogram of the percent
error in fuel economy for the A3 vehicle. This
histogram shows the percent difference
between the simulated fuel economy and the
measured fuel economy across all of the laps,
both ATEF and Churchville-C. The mean
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percent error is about 1.2%, but the standard deviation of the percent error is 5.5% percent. This indicates that the percent error is spread out over a wide band, although the mean error of the simulation is small. The reason for this is threefold: lap-to-lap variability due to the human driver, variability in the surface conditions of the gravel road, and variability due to uncertainty in the grade.





Figure 26 is a histogram of percent error that illustrates the reduced variability in the percent error when considering only laps driven by the AMAS and smart cruise over flat, paved roads. In this case, the mean error indicates the result is still biased by -2.4%, but the standard deviation of the percent error has dropped significantly. This dramatic decrease in variability can be attributed to excluding the following three conditions: any lap driven by a human driver, any lap driven on a gravel road, and any lap with a variable grade.



Figure 26: Histogram of Percent Fuel Economy Error for A3 AMAS and Smart Laps

Figure 27 shows similar results for the A5. The mean error is low, but the variability is high.



Figure 27: Histogram of Percent Fuel Economy Error for A5

Figure 28 shows similar results when the analysis is limited to the AMAS or smart cruise on flat paved roads.



Figure 28: Histogram of Percent Fuel Economy Error for A3 AMAS and Smart Laps

The vehicle model calibrated using the test data is more accurate than the original model used to design the first phase of the smart cruise control. Even though the model was less accurate during the first iteration, it still enabled the controller development to proceed, yielding a controller that improved the fuel economy. We expect that this refined vehicle model, calibrated using the test data, will yield an even better controller for the second phase. Having a more accurate vehicle model will also make calibrating the controller in simulation easier, thereby reducing the overall calibration time in the vehicle.

NEXT STEPS

The next steps of this project will involve using a distance horizon and creating a model predictive control (MPC) using the vehicle model correlated to the test data. Figure 29 shows how the MPC will look ahead and optimize fuel economy over the horizon [5].



Figure 29: Model Predictive Controller over a Horizon

In addition, the vehicle will be tested as part of a convoy during the next round of vehicle testing.

CONCLUSIONS

For this study, a smart cruise controller was developed and calibrated in simulation for two Class 8 trucks: a M915 A3 and a M915 A5. We then ran the smart cruise control as part of the HIL/SIL system and later used it in test vehicles on the ATEF and Churchville-C courses. Fuel economy improvement was demonstrated for the smart cruise control on the ATEF course. However, no fuel economy improvement was shown for the Churchville-C Course, primarily because of the limited availability of information about the route during testing. This issue will be addressed in future testing by providing a grade horizon up to 200 meters in front of the vehicle. The test data that was collected from this first round of testing was correlated with the vehicle models and used to improve the accuracy of the model. This will help in the development of the MPC.

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DEFINITIONS/ABBREVIATIONS

K_p	Proportional gain for the PI
-	controller
K_i	Integral gain for the PI
ţ.	controller
V^*	The vehicle speed which
	minimizes the cost
V	The set of all admissible
	vehicle speeds
V_{driver}	The given set speed set by
	the driver
V_{target}	Target speed for the PI
	controller
V	Vehicle speed
ΔV	Vehicle speed tolerance
t	Time
Т	The time period over which
	the cost function is evaluated
ω_{eng}	Engine speed
T_{dmd}	Torque demand at the wheels
T_{eng}	Torque at the engine
\dot{m}_{fuel}	The mass flow rate of the
,	fuel
C_{rr0}	The first-order rolling
	resistance coefficient
C_{rr1}	The second order rolling
	resistance coefficient
θ	Grade angle
A	Frontal area of the vehicle
C_d	Coefficient of drag
δ_{air}	Air density
g	Acceleration due to gravity
m	Mass of the vehicle
R_{wheel}	Rolling radius of the wheel
R_{fd}	Ratio of the final drive
Rtrans	Ratio of the transmission as
	a function of gear number
N_{gear}	Gear number
η_{fd}	Efficiency of the final drive
η_{trans}	Efficiency of the
101 0100	transmission